

Fluid Mechanics and Hydraulics Machines Prepared by

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4th Semester Diploma

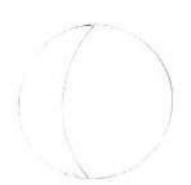
Department of Mechanical Engineering

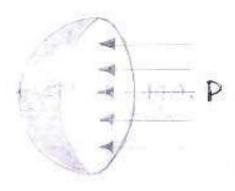
(11) Pressure borece on the area of d2 = PX To d2 as shown in figure. These two borces will be equal and opposite under equilibratum conditions. The.

$$P = \frac{G \times \pi d}{\pi \times d^2} = G \times \pi d$$

$$P = \frac{G \times \pi d}{\pi \times d^2} = \frac{46}{d} \longrightarrow \frac{1}{2}$$

The above equation shows that with the decrease of diameter of the droplet, pressure intensity inside the droplet increases.





(0) Droplet

(B) Sunface (FORCES ON DROPLET

(C) PRESSURE FORLLES

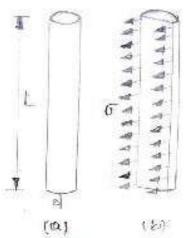
SURFACE TENSION ON A LIQUID JET =

Consider a lequid set of diameter of and tength "L" as shown in Figure.

Let p= pressure intensity inside the liquid Jet above the outside Pressure

U = Surface tension of the liquid Consider the equilibrium of the Semi set, we have force due to Pressure - px ranea of semi set = PX LXd

torce due to surface tension = 0x2L



FIREES ON LIQUID

Equating the forces, we have $p \times L \times d = \sigma \times 2L$ $\Rightarrow P = \frac{G \times 2L}{L \times d}$

SURFACE TENSION ON A HOLLOW BUBBLE of A Hollow bubble like a some bubble in air has two surfaces in contact with air, one inside and other outside. Thus two surfaces are subjected to surface tension. In such case, we have

- CAPILLARITY :-

or Capillarity is defined out a phenomenon of the orthogen of liquid when the tube is held vertically in the liquid. The tise of liquid surface is known as Capillary tise while the ball of the liquid surface is known as Capillary tise while the ball of the liquid surface is known as Capillary degrees.

of It is expressed interms of Cm on mm of liquid. Its value defends upon the specific weight of the liquid, diameter of the tube and sunface tension of the liquid.

Expression for Capillary Rise:

Consider a glass tube of small diameter of opened out both ends and is insented in a liquid, say water. The liquid will rise in the tube above the level of the liquid.

Let he height of the liquid in the tube. Under a state of aquilibrium, the weight of liquid of height his balanced by the force of the surface of the liquid in the tube. But the force at the surface of the liquid in the tube is the tube to surface of the liquid in the tube is the

Let G = sunface tension of liquid 0 = Angle of Contact between liquid and glass tube The weight of liquid of height h in the tube = (Arrea of tube xh) = #d3xhxpxg - 1 (CAPILLARY RISE) when P = Density of liquid Vertical component of the surface tensile force = (X circumberence) X cos B = TX nd x cos 0 For equilibrium, equating (1) & (2), we get The dah por = TXTE x cos on The TARDX COS B = 40 COS B - 3

The value of 0 between water and clean glass tube is approximately equal to zero and hence cos a is equal to unity. Then rise of water is given by

h= 45 - 9

Expression for Capillary Fall:—

Et the glass tube is dipped in mercury, the level of mercury in the tube will be lower than the general level of the Cutside Inquid as shown in the figure.

Ket Mattelght of depression in tube

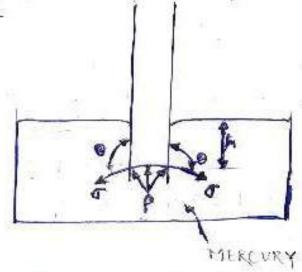
Then in equilibrium, two forces one acting on the mercury inside the tube. First one is due to surface tension acting in the downward direction and is equal to FX tol x cos a.

Second boace is due to hydrostatic boace acting upward and is equal to intensity of pressure at a depth hix Arrea

= PX \(\frac{1}{4} a^2 = pg xhx \frac{11}{4} a^2 \\
(" P = Pgh)

Equating the two, we get $G \times \pi d \times \cos e = pgh \times 7 d^2$ $\Rightarrow h = 46 \cos R$ pgd

.. Value of 0 for mercury, and glass tube is 1280.



(CAPILLARY FALL)

Consider a small Area of in large mass of bluid. It the bluid is stedionary then the force exerted by the surrounding bluid on the area of will always be perpendicular to the surface of .

Let of is the force earling on the area of in the normal direction. Then the matio of $\frac{dF}{dA}$ is known as the intensity of Pressure on Simply pressure and this reation is represented by P. Hence mathematically the pressure at a point in a bluid at rest is $p = \frac{dF}{dA}$

It the Force (F) is uniformly distributed over the Area (A), then pressure at any point is given by

: Force or pressure force, F= PXA.

The unit of pressure are it kgt/m² and kgt/cm² in MKS unit.

(ii) Newton/m² on N/m² and N/mm² in II unit.

N/m² is known as pascal and is represented by Par

other Commonly used units of pressure are:
kpa = kilo pascal = 1000 N/m2.

bar = 100 kpa = 105 N/m2.

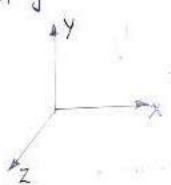
PASCAL'S LAW >

It states that the pressure on intensity of pressure at a point in a static bluid is equal in all directions.

This is proved as!

The fluid element is of very small dimensions.

ie da, dy and dl .



Px.oly.1 da c

(FORCES ON A FLUID ELEMENT

Consider an arbitrary bluid element of wedge shape in a bluid made at nest as shown in bigure. Let the width of the bluid made at nest as shown in bigure. Let the width of the element pierpendicular to the plane of paper is unity and pa, by and Pz are the pressures on intensity of pressure acting on the face AB, AC and BC respectively. &

Let LABC = 0, then the forces acting on the element are:

- (1) Pressure forces normal to the surfaces and
- (2) Weight of element in the ventical direction.

The forces on the faces one :-

Force on the face AB = PXX Area of face AB = PXXAyX1

Similarly force on the bace AC = Pyxdx X I

borce on the bace BC = Pz xds X 1

weight of element = (Mais of element) x g

= (Volume x p) x g

= (AB x AC x 1) x p x g

where P= olensity of bluid

Resolving the borces in x-direction, we ha

Resolving the borces in X-direction, we have

Px Xdy X1 - P(ds X1) sin(900-0) = 0

Px Xdy X1 - Pzds X1 cos D = 0

on But from bigune, ols coso = AB = dy

Px xdy xL - Pzxdy x1 = 0

Px = Pz

on similarly, resolving the borces in y-direction, we get

by xdxx1-px xds x Less (90-0) - dxxdy x1 x f xg=0

y pydx + pzds sin 0 - dxdy x f xg = D

1 DR/. Let the width of the elements is 1 Hence

the area of bonce on face AB = dy x 1 (FAB = Pyxdyxi)

area of bonce on face AC = dx x1 (FAC = Pxxdxxi)

area of bonce on face BC = dx x1 (FBC = Pxxdxxi)

Weight of element = (mase of element) x g
= f x values x g
= f x (\frac{1}{2} AC x AB x 1) x g

For equilibraium

Considering the body at equilibraium

Resolving the left and right borces.

FAS = FBC COS O -> Py. dy. 1 = Px ds 1 cos 0 => py, dy = Pz, do tos os + cos 10 = MB x dy -> ds cos o = dy

Applying this in the expection Py.dy = Pz.dy

wpy = Pz - 0

Resolving the up boreses and down boreses FAC = FBC, Six 0 + 10

> => Px dx -1 = Pz ds 1. sins + fx(2-dx; dy 1) x g of Pada = Pads sir 0 + fg dady

as da, dy will be very small, Hence I can be neglected. Applying in the equation

Pa, da = Pz da => Px=Pz

: Px=Pn=Pz -- 0

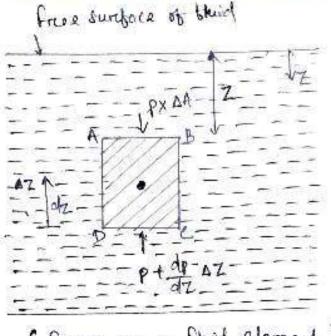
PRESSURE HEAD & HYDROSTATIC LAW :+

The pressure out any point in a bluid at rest is obtained by the Hydrostatic Law which states that the rate of increase of pressure in a ventical observant direction must be equal to the weight density of the blund out the points

Let AA = Cross Sectional Acea AZ = Height of bluid element

P = pressure on face AB

Z= Distance of bluid element from bree surface W = weight density of bluid



(forces on a fluid element)

for equilibrium

$$D + (P \times \Delta A) = (P + \frac{dP}{dz} \Delta Z) \Delta A$$

$$\Rightarrow [P(\Delta A + \Delta Z)g] + P \times \Delta A = (P + \frac{dP}{dz}) \Delta Z \cdot \Delta A$$

$$\Rightarrow P \cdot \Delta A \cdot \Delta Zg + P \cdot \Delta A = P \cdot \Delta A + \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A$$

$$\Rightarrow P \cdot \Delta A \cdot \Delta Zg = \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A$$

$$\Rightarrow P \cdot \Delta A \cdot \Delta Zg = \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A$$

$$\Rightarrow P \cdot \Delta A \cdot \Delta Zg = \frac{dP}{dz} \cdot \Delta Z \cdot \Delta A$$

This equation is known as Hydrostatic Law.

$$\frac{d\rho}{dz} = fg$$

$$\Rightarrow \int d\rho = \int fg dz \qquad \left(\begin{array}{c} \cdot \cdot \cdot Z = \frac{P}{fg} \end{array} \right)$$

$$\Rightarrow P = fgZ$$

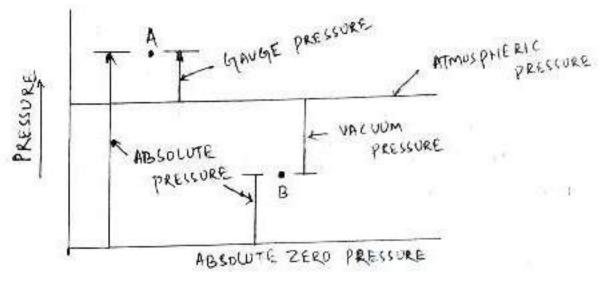
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TYPES OF PRESSURES !-

- or the pressure on a bluid is measured in two different systems. In one system, it is measured above the absolute Zerco on Complete, Vacuum and it is called the absolute pressure and in other system pressure is measured above the atmosphereic pressure and it is called gauge pressure. , There are different types of pressure in this system.

 - 1 Absolute pressure
 - 3 Gauge Pressurce
 - 3 Vacuum pressure
 - (1) Absolute Pressure ? Of is defined as the pressure which is measured with the help of a pre reference to espectate vacuum pressure.
 - (3) Equipe Pressure -> It is defined as the pressure which is measured with the help of a pressure measuring instrument, in which the atmospheric pressure is taken as datum. The atmospheric pressure on the scale is marked as Zerro.
- 3 Vacuum Pressure => It is defined as the pressure below the atmospheric Pressure .
 - The relationship between the absolute pressure gauge. Pressure and vactum pressure are shown in figure below. Mathematically ,
 - (i) Absolute pressure + Gauge pressure + Atmospheric Pressure ore Palo = Patro # Pgauge

(fi) Vacuum Pressure - Atmospheris pressure - Absolute pressure - 7 Pval = Palm - Pab



[Relationship between Pressures]

MEASUREMENT OF PRESSURE 9

The pressure of a bluid is measured by the following devices:

1. Manometers 2. Mechanical Gauges

(1) MAHOMETERS 7

Manometers are defined as the devices used box measuring the pressure at a point in a blud by balancing the column of built by the same on another column of the bluid. They are classified as:

(a) simple manamedens

(b) Differential Manomelers

(2) MECHANICAL GAUGES 9

the pressure by belancing the build column by the spring or dead weight. The commonly used mechanical pressure gauges are:

(a) Diaphragm Pressure gauge (c) Dend-weight pressure gauge
(b) Boundon tube pressure gauge (d) Bellows Pressure gauge

1 calculate the dencity, specific weight and weight of

m = 3 m = 3

V= 1 lil = 10-3 m3/103 (m3 S = 0.7

S = whoy = for y

\$S = floq looky |m3

7 0.7 = floor kg/m3

3 -f lig = 65000 7 × 1000 = 700

W= fxg = 700 x 9.81 = 6867 N/m3

W=mg = fx xxg

= 700 XVX9.8 = 700 X 10-3 X9.81

W = 6867 X 10-3 = 6.867 N

(Ans)

Q.3 Two horizontal plate care place 1.25 (m apart from each other 2 the space between them is filled with oil of viscosity 14 poise. Calculate the shear stress in oil & it the upper plate is moving with a velocity of 2.5 mgs.

 $M = 1.25 \text{ cm} = 1.25 \times 10^{-2} \text{ m}$ $N = 14 \text{ poise} = 14/10 = 1.4 \text{ N/m}^2$ $V_2 = 2.5 \text{ m/s}$

91=D

13 Find the kinemetic Viscocity & specific greatly of an oil having density of 981 kg/m3. The shear stress out a point in oil is 02452 N/m2 & velocity gradient is given by 0.2/sec.

(My)
$$f = 981 \text{ kg/m}^3$$
 $7 = 0.2452 \text{ N/m}^2$
 $5 = 7$
 $\frac{du}{dy} = 0.2/sec$
 $\frac{du}{dy} = \frac{1226 \text{ NS/m}^2}{1000}$
 $\frac{du}{dy} = \frac{1226 \text{ NS/m}^2}{1000}$

Get The relocity distribution from flow over a floot plate is given by U=3/4y-y2 in which U is the velocity in m/s 2 y is the distance in metre above the plate Determine the shear stress at y=1.5 m & the dynamic viscosity at 8.6 poise

\$ ch of y =1.5 m

then,
$$\frac{du}{dy} = \frac{3}{4} - \frac{3}{4} = \frac{3}{4} = \frac{3}{4} = \frac{-9}{4} = -2.25$$

: SIMPLE MANDOMETERS

A simple manometer consists of a glass tube having one of its ends connected to a point where pressure is to be measured and other end remains open to admosphere. Common types of simple manometers are:

(1) piezometer .

(3) U-tube manometers and

(3) Single Column manometer.

4) PLEZOMETER >

Det is the simplest from of manometer used bor measuring gauge pressures. One end of this manometer is connected to the point where pressure is to be measured and other end is open to the

almosphere as shown in bigune,

Bressure head at that point.

It dot a point A, the height of liquid

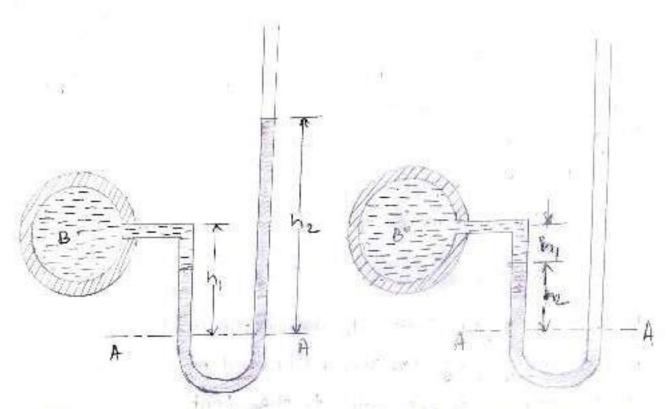
say who water is h in presometer tube, then pressure at $A = \frac{1}{10} \times 9 \times h \frac{10}{m^2}$

Prezo meder

(2) U-TUBE MANOMETER =>

It consists of glass tube bent in U-shape, one end of which is connected to a point at which possessure is to be measured, and other end remains open to the atmosphere as shown in & the bigure. The tube generally contains mercurey ore any other liquid whose specific gravity is greater than the specific gravity

Of the liquid whose pressure is to be measured.



(a) For Gauge pressure

(b) For Vacuum pressure

(A) FOR GAUGE PRESSURE =>

Let B is the point out which pressure is to be measured, whose value is p, the dadum line is A-A.

Let his height of Right liquid outsove the doctum line

haz height of theavy liquid above the datum line

SI = Specific growty of layout liquid

fit Darsity of light liquid = 1000 x Si.

Sz = Specific growny of heavy liquid

P = Denuty of heavy liquid = 1000 XS2

As the pressure is the same for the horizontal surface, Here pressure above the horizontal doctum line A-A in the left court and in the right column of V-tube manameters. Should be sime

Pressure above A-A in the right column = P+P+xgxh,
Pressure above A-A in the right column = P2×gxh2

Hence repeating the two pressures. p+pigh = fighz > P= P29h2-Pi3h1 - (1)

(B) FOR VACUUM PRESSURE => For measuring vacuum pressure, the level of the heavy liquid in the manometer will be as shown in the above briguize. Then pressure above 4-4 in the left column = fight Pightp pressure head in the right column above A-A = 0 1. Hence Paghet Pighi+P=D 7 P=- (2)

[3] SINGLE COLUMN MANOMETER =>

Single Column manameter is a modified from of a U-tube manometers in which a reservior thowing a large cross-sectional area (about 100 times) as compared to the area of the tube is Connected to one of the limbs (say left (mb) of the manometer as shown on bigune. Due to large exist-sectional area of the reservoor, bor any variation in pressure, the change in the liquid level in the reservaire will be very small which maybe neglected and thence the pressure is given by the height of liquid in the other limb. The other limb may be vertical on inclined. Thus there are two types of single column manometer as; (1) Vertical single column marximeters

(2) Inclined single column manometers

(1) VERTICAL SINGLE COLUMN MANDMETER ?

The bigure shows the ventical engle column manometer.

Let X-X be the datum line in the reservoire and in the reight line of the manometer, when it is not connected to the pipe, when the manometer is connected to the pipe, when the manometer is connected to the pipe, due to high pressure out A, the heavy loqued in the reservoire will be pushed downward and will risk in the reight limb.

Let Ih = fall of heavy liqued in

hz = Rise of heavy lequid in right limb hi = Height of Centre of Pipe 7 outpove X-X

PA=Pressure at A, which is to be measured

A - Cross. sectional Area of

a = Creats_sectional area of the reight lamb

Si = Sp. gravity of liquid in pipe

Sz = Sp. grawty of heavy liquid in reservoir and right Himbs

Pr = Dansity of legical in pape

fz = Denaty of toquid in nesenvoin

Fall of heavy liquid in reservior will course a ruse of heavy liquid

 $A \times \Delta h = \alpha \times h_2$ $\Rightarrow \Delta h = \frac{\alpha \times h_2}{A} \qquad (0)$

Now consider the doctum line Y-Y as shown in biquie, then pressure in the reight timb above Y-Y.

= f2 x gx (bht h2)

pressure in the left lamb above Y-Y = fix gx (shthi) + pa

Equating the pressures, we have $f_2 \times g \times (\Delta h + h_2) = P_1 \times 1 \times (\Delta h + h_1) + P_A$ $\Rightarrow P_A = P_2 g (\Delta h + h_2) - P_1 g (\Delta h + h_1)$ $\Rightarrow \Delta h (P_2 g - P_1 g) + h_2 P_2 g - h_1 P_1 g$

But from equation (i) , $\Delta h = \frac{a \times h_2}{A}$

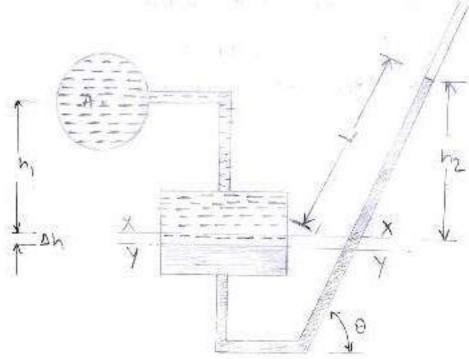
=> PA = axh2 [f2g-f19]+ hzf29- hif19 ----

As the area A is very large as compared to a hence traffor a becomes very small and can be neglected.

Then Pa = h2/29- h, fig :

from Loquetion not is clear that as he is known and hence by knowing he or raise of heavy liquid in the right limb, the pressure at A can be reglected Calculated.

[3] INCLINED SINGLE COLUMN MANDMETER >



The biguite shows the inclined single column manometer. This monometer is more sensitive. Due to inclination the distance moved by the heavy liquid in the reight limb will be more.

Let L = Length of heavy liquid moved in reight limb from X-X

0 = Inclination of reight limb with horizontal

hz= Ventical ruse of heavy loquid in reight limb from X-X = LX sing

from equation, the pressure at A is

PA = h2f2g - h1f1g

Substituting the value of h2, we get

PA = Sin D x f2g - h1f1g

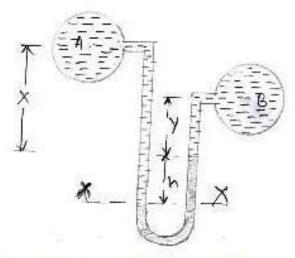
: DIFFERENTIAL MANDMETERS :-

Differential manomaters are the devices used for measuring the difference of pressures between two points in a pipe or in two different pipes. A differential manometer consists of a U-tube, containing a heavy liquid, whose two ends are connected to the points, whose difference of pressure is to be measured. Most comming types of differential manometers are:

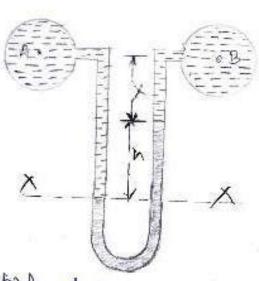
- (1) U-tube differential manometer and
- (3) Envented U-tube differential manometers

(1) U-TUBE DIFFERENTIAL MANOMETER 7

The figures shows the differential manometers of U-tube type.



Coutwo pipes and distancent levels



(b) A and B are at same level

and also content logarids, of abbanent specific greavity. These points are connected to the U-tube differential manuscript. Let the pressure at A and B over Pa and Pa

Let he subsenence of meneury level in the U-tube,

y = Distance of the centre of Bitnom the more carry level in the night limb

X= Distance of the centre of A, brom the mercury level in the right limb

Pi = Density of liquid of A.

f2 = Density of liquid at B

fy = Density of heavy legald of mercany

Taking datum line of X-X.

Prossure above X-X in the left limb = f,g(h+x)+PA

where PA = Pressure at A.

Pressure above X-X in the right limb = fgxgxh+p2xgxy+p3 where PB = pressure of B;

Equating the two pressure, we have

fig(htx)+PA = fgxgxh+f2gy+fB > PA-PB = fgxgxh*+f2gy-fig(h+x) = hxg(fg-fi)+f2gy-figx

Difference of pressure at A and B = hxg(fg-f1)+f294-f19x

Enfigure (b), the two points A and B are ed the same level and contains the Sume liquid of density for them

Pressure above X-X in right limb = fox g x h +fox g x x + po

Pressure above X-X in left limb = fox g x (h+x)+ Pa

Equating the two pressure

fg x g x h + P, gx + Ps = f, x g x h + x) + PA

=1PA-PB=+fg x g x h + f, gx - F, g (h + x)

= g x h (-B, -f)

[2] INVERTED U-TUBE DIFFERENTIAL MANOMETER-

It consists of an invended U-those containing a light liquid. The two ends of the two are connected to the points whose difference of pressure is to be measured. It is used for measuring difference of low pressures. The figure shows on invended U-tube differential managing Connected to the two, points A and B. 1801

Let the pressure at A is more than the pressure at B.

Lat hi= height of liquid milettimbs
below the doctor line X-X

hz=Height of liquid in relightlimb X h=Dibberrence of light liquid

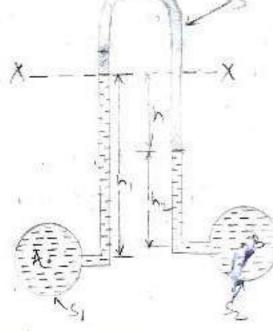
ti= Density of Deput of A

fz = Dansity ob liquid out B

Ps = Density of trapped light liquid

·PA = present at A

PB = Pressure out B



Taking X-X as datum line, then pressure in the left limb below X-X = PA-P, Xg Xh,

Presistance in the right limb below X-X
= RB- P2X 9 X h2- P5X 9 X h

Equating the two pressure,

PA-fixgxhi=Ps-tzxgxhz-tsxgxh

>1PA-PB=fixgxh1-f2xgxh2-f3xgxh

Questions?

(4) A simple V-tube monometers is used to measure the pressure of worders in a pipe line which is above the estimospheric of worders the wight timb obtain monometers contains moneung it is upon to the older pressure A the contact between u the big determine the pressure of moneung seconds is to the less that we shall interest the the second the less of the

tig is not the same level on the center of the pipe? Ons) PATP19h1 = Paghe

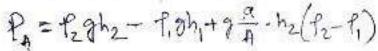
=>PA + (1000 × 9.81 × 10 × 10-2) = (13.6 × 1000 × 9.81 × 100 × 10.2) =>PA = (1000 × 9.81 × 1000 × 9.81 × 1000 × 9.81 × 1000 × 9.81 × 10 × 10-3)

7 PA = 133416- 981 = 12360.6 N/m² (Ans)

(3) A single column monometer is connected to a pape containing a liquid of specific flavity or as shown in biguing. find the pressure on the pape it the area of the mercentain is looking the area of the mercentain is looking the area of the fire area of the fire area of the fire area of the mercentain is looking the area of the area of the fire area of the containing the area of the area of the fire area of the fire area of the area

20

(Ans) $h_1 = 20 \, \text{cm} = 0.20 \, \text{m}$ $h_2 = 40 \, \text{cm} = 0.4 \, \text{m}$ $f_1 = 0.9 \, \text{x} \, 1000 = 900 \cdot$ $f_2 = 13.6 \, \text{x} \, 1000 = 13600$ $f_2 = 9.81$





A=lova

=100

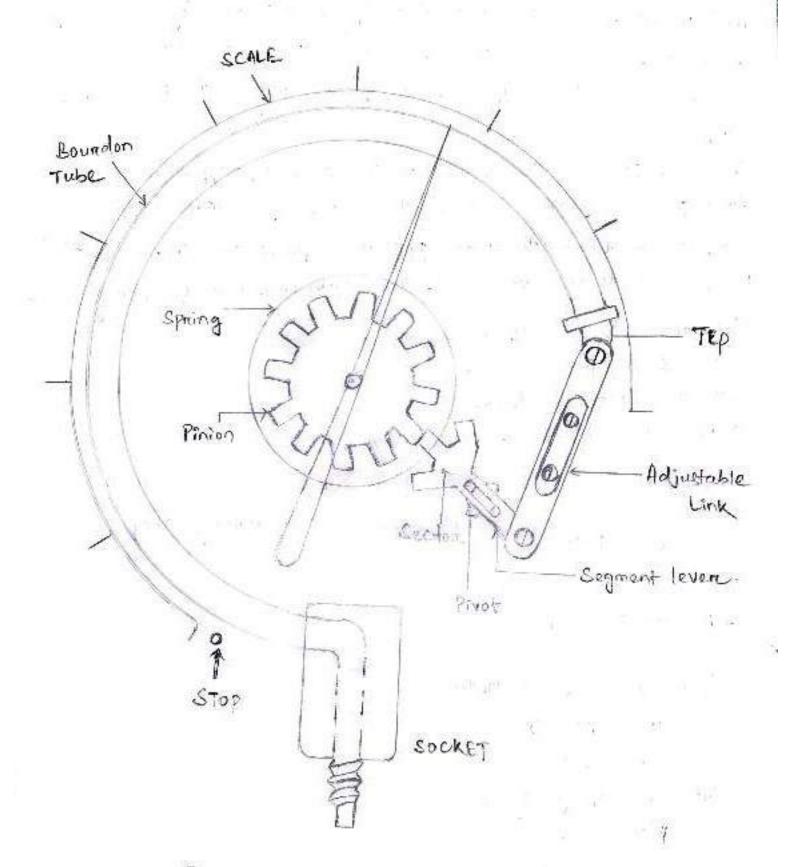
= 13600x9,81 x0.4-900x9.81 x0.21+ 9.81 x 100 x0.4(13600-900) = 53366.4-17658+0.03924 x 12700

= 35.708.4 4498.348

= 36206-748 N/m2 (Ans)

BOURDON TUBE PRESSURE GAUGE

- Theoreton tube pressure gauges are classified as mechanical pressure measuring instrument, and thus operate without any electrical power. This type of pressure gauges were first developed by E. Bourdon in 1849.
- 7 Bounday tubes one madially formed tubes with an oval
- Thousand tube pressure gargages can be used to measure over a wide mange of pressure form various to pressure as high as few thousand psi.
- 7 It is basically consisted of a C-shaped hollow tube, whose one end is fixed and connected to the pressure tapping, the other end tree.
- -7-The Cross Section of the two is elliptical. When pressure is applied, the elliptical tabe (Bounder tube) tries to acquire a cincular Cross-Section, as a result, Stress is developed and the two tries to Stresgitten up.
- magnitude of pressure.
- This motion is the measure of the pressure and is indicated via the movement of a deflecting and indicating mechanism is attached to the bree end that retates the pointer and indicates the pressure reading.
- orthe materials used are commonly phosphore Bronze, Breaks and Berrylloum, Copper.
- tubes, such as helocal, twisted on spiral tubes are also in use.



[BOURDON TUBE PRESSURE GAUGE]

CHAPTER - 03 TOTAL PRESSURE AND CENTRE OF PRESSURE =

or Total pressure is defined as the force exercted by a staticity on a sunface esther plane on Curved when the blued in contact with the sunfaces. This force always acts normal to the Surface "

-7 Centre of pressure is defined as the point of application of the total pressure on the sunface. There are four cases of Submerg Sunfaces on which the total pressure force and centre of pressure is to be determined. The Submerged sunfaces may be ;

(1) Vertical plane Surface

- (2) Horizontal plane surface
- (3) Inclined plane surface
- (4) Curved surface

(1) Ventical plane sunface submerged in Liquid of

Consider a plane Ventical surface of consisterary shape immercial in a liquid as shown in biguire.

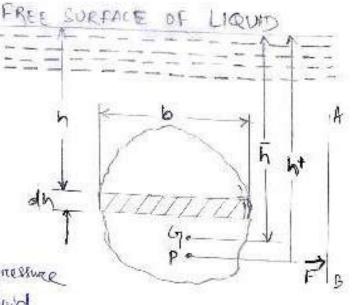
Let A = Total area of the Surface_

> h 7 Distance of C.G. of the anea brown breez surface of lequid

G = central of growity of plane Surface.

P = centre of pressure

W = Distance of Centre of pressure perom peer rankence of reducid



(a) TOTAL PRESSURE (F) :-

The total pressure on the surface may be determined by deviding the entire surface into a number of small parallel strips. The force on Small strip is then calculated and the total pressure bonce on the whole area is calculated by integrating the force on Small strop;

Consider a strap of thickness with and width to at the depth of h brom bree surface of liquid as shown in biguine.

pressure intensity on the strip, p=figh Area of the strip, dA = bxdh

Total pressure borce on strip, df = px Area = fghxbxdh

. Total pressure force on the whole surface,

F= fdF=ffghxbxdh=fgsbxhxdh

But Soxhxdh = ShxdA

= moment of surface cinea about the bree Surface of logical

- Arrea of surface × Distance of e.g. 5mm the brice surface

= AX h

1. F= Pg AT

I force would be in Newton.

(b) Centre of Pressure (h') :-

Centre of pressure is calculated by using the principle of money, which states that the moment of the resultant bonce about an axas is equal to the sum of moments of the components about the same axis.

The resultant force F is acting at p, at a distance hi brombree surface of the legal as shown in figure. Hence moment of the borce F about three surface of the liquid = F x h' — (1)

Moment of force of, acting on a strip about bree surface of legal = df x h

[: df = pqh x b x dh]

= fqh x b x dh x h

Sum of moments of all such borces about free Surface of liquid

= offices (fghxbxdhxh

= fg (bxahxholh

+ Pa (usu)

= 9 Sthtah (": bah = dA)

But ShadA = Sbhadh

= moment of Ineration of the surface about the free surface of legal = Io

: Sum of moments about bree surface = fg10 - (2)

Equating (1) and (2), we get

FX h' = fg20 But = F = fgAh

:. fgmx h = fg10

 $\Rightarrow h' = \frac{fg\tau_0}{fgAh} = \frac{\tau_0}{Ah} \qquad (3)$

By the theorem of parallel axis, we have Io = Total Ax h2

where In moment of Inentice of the about an axe passing through the city of the anen and parallel to the free surface of legald.

Substituting To in equation (3), we get $h' = \frac{I_0 + Ah^2}{Ah} = \frac{I_0}{Ah} + h \qquad (4)$

In egn 14), it is the destance of cigob the area of the ventical surface from the surface of the liquid. Hence from equation (4), it is clear that

(1) Certae of passione (i.e. h!) has bottom the certae of gravity of the vertical surface.

(ii) The distance of centre of pressure been three surface of liquid is independent of the density of the liquid.

The Moments of Inertia and other geometric properties of Some Important Plane Surfaces:

plane surface	C.G. brom	Arren	Moment of Inerctic about an axis passing through E by, and Parallel to bate (Iby)	t doment of ineration about base (ID)
1. Rectangle	x = \frac{d}{2}	Ьď	bd3 12	2 3 3
7. Traingle	x= 1/3	<u>bh</u> 2	<u>bh³</u> 36	443 12

Plane Sunface	Cog. brom the Base	Ane a	stoment of mentice about an axis passing through C.G. and parallel to base (Ig)	Moment of Ineration abo base (Ib)
3. Cincle	α= d/2	742 4	TING TO	
4. Fragezium	2 = (2 a+b) h	(a+b) x h	(a2+4ab+b2)xh3	

ARCHIMEDES' PRINCIPLE

- of When an object is completely on particulty immensed in a bluid, the bluid exents an appeared borce on the object equal to the weight of the bluid displaced by the object.
- of when a solid object is wholly on printly immersed in a blood, the bluid molecules are continually striking the Submerged Surface of the object. The force due to these impacts can be combined into a single borce the buoyant force. The immersed object will be lighter ite. It will be buoyed up by an amount equal to the weight of the build it displaces.

BUOYANCY >

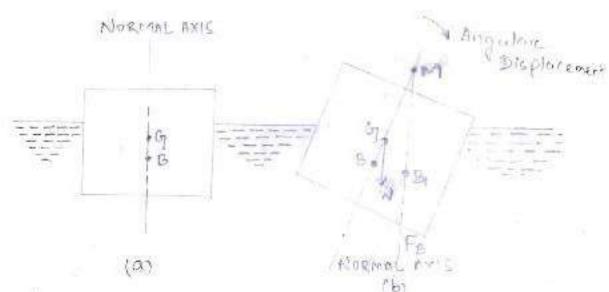
When a body is immensed in a bluid, an upround bornce is exented by the bluid on the body. This upward bornce is equal to the weight of the bluid displaced by the body and is called the bornce of belogancy on Simply buoyancy.

CENTRE OF BUDYANCY :-

It is defined as the point, through which the force of buoyancy is supposed to act. As the force of buoyancy is a vertical force and is equal to the weight of the fluid displaced by the body, the Centre of buoyancy will be the centre of gravity of the fluid displaced.

oscillating when the body is tilted by a small angle. The meta-current may also be defined on the point at which the line of action of the force of bouryancy will meet the nound axis of the body when the body is given a small angular olisplacement.

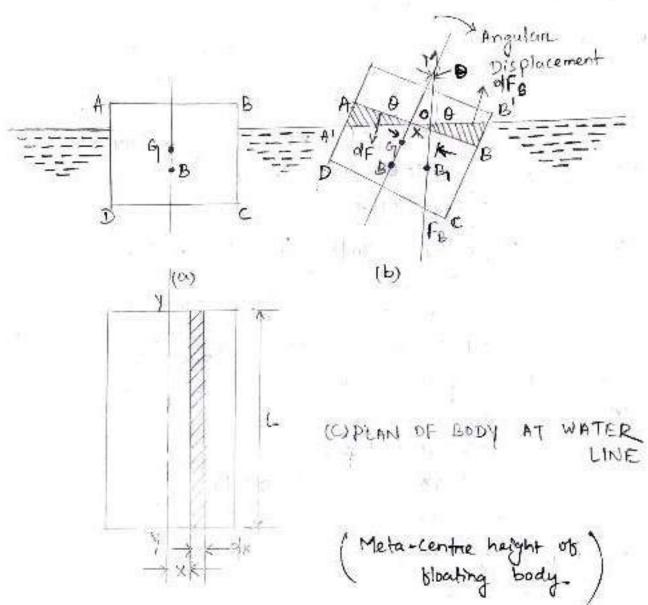
The Considere or body bloating in a liquid as shown in figure. Let the body is in equilibrium and by is the centre of greavity and bithe Centre of buoyancy. For equilibrium, both the points lie on the normal axis, which is Nentical.



Let the bedy is given a small angular displacement in the clockwise direction as shown in bigure (a). The Centre of buoyancy, which is the centre of gravity of the displaced liquid on Centre of gravity of the poster of the body sub-merged in liquid wall now be shifted towards right from the normal axis, Let it at a as shown in bigure (b). The line of action of the force of buoyancy in this new position, will intensect the normal axis of the body out some point say M. This point M is called Meta-Centre.

META-CENTRIC HEIGHT &

The distance Mg, i.e. the distance between the meta-centre of a bloating body and the centre of gravity of the body is called meta-centric height.



Comple Due to Wedges :-

Consider towards the right of the axis a small strop of thickness also at a distance of a from D as shown in bigkb.

The height of strop ** X LBOB! = X X O (:: LBOB! = LAOA! = BMB! = 10)

2. Arrea of strap = Height X Thickness = XXBXdX

96 L is the length of the bloating body other

Volume of strap = Arrea X L

= XXBXLXda

*. Weight of strop = if g x volume = for oldar

Simplantly, it a small strip of thickness du at a distance or from O to wands the left of the axis is considered, the weight of strip up be flynould a. The two weights one outling in the apposite direction and hence constitute a couple.

Moment of this emple = Weight of each strop x Distance between these two weights

= four Lan x 2n = 2 fgn2 ol da

:. Moment of the couple for the whole wedge = \$2590x2 a Late -(1)

Moment of couple due to shifting of Centre of buoyancy trum

B to B | = FB x BB |

= FB x BM x 0 (-1 BB = IBM x 0 if 0 is very

= W x BM x 0 —(2) (FB = W)

But these two couples care the same thence equating equations

WXBMXB = Separzolda NXBMXB = 12Pgo Sarabalda NXBM = 2Pg Sarlda

Now Lange Elemental arrest on the water fine shown in figure (c) and = all

is MX BW = 368 las oft

But from figure (c). it is clear that 2 (n2 old is the second moment of area of the plan of the body out whater surface cubout the axis y-y. Therefore

WXBM=fgE => BM= fgI W (where L = 2 for 2014)

But 'W = weight of the body

= weight of the bland dispinced by the body

= 49 x Volume of the bland displaced by the body

= fg x Volume of the body Sub-merged in water

= fg x V

: BM = \frac{4}{7}xI = \frac{1}{4} - (3)

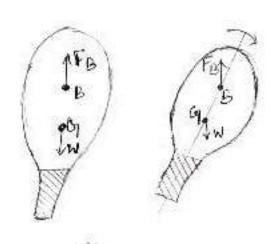
GM = BM - BG = \frac{1}{4} - BG = \frac{1}{4} - BG = (4)

: Metal Central height = GM = \frac{1}{4} - BG = (4)

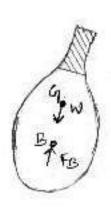
CONDITIONS OF EQUILIBRIUM OF A FLOATING AND
SUB-MERGED BODIES

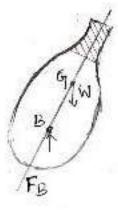
A sub-merged on a floating body is said to be struble it it comes back to its original position extent a slight disturbance. The relative position of the centre of gravity (6) and centre of buoyancy (81) of a body determines the Stability of a sub-merged body.

The position of Centre of gravity and centre of buoyancy in case of a Completely submerged body are fixed. Consider a balloon, which is completely submerged in air. Let the lower portion of the bearganty balloon centains heavier material. So that its Centre of gravity is lower than its centre of buoyancy as shown in figure (a). Let the weight of the balloon is W. The weight Wis acting through by verifically in the douonicand direction, while the browgant force Fo is acting verdically up, through B. For the equilibrium of the balloon w= Fo. If the balloon is given an angular displacement in the Clockwise alirection as shown in biguit (a), then w and Fo konstitute a couple acting in the anti-clockwise alirection and brings the balloon in the original position. Thus the balloon in the position, shown by biguite (cy is in Stable equilibrium.

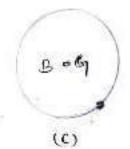


(4) STABLE EQUILIBRIUM





(b) EQUILIBRIUM UNSTABLE



NEUTRAL EQUILIBRIUM

(Stabilities of Jub-marged bodies)

(a) Stuble Equilibrium -

When W= Fg and point is is above by, the body De said to be in stable equalibrium.

(b) Unstable Equilibrium 1—

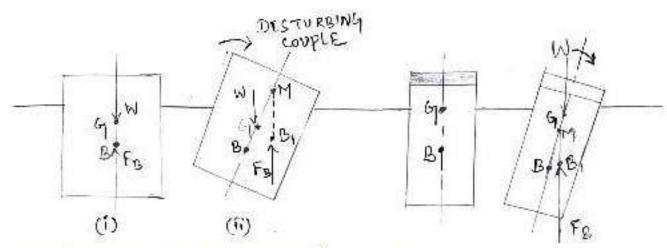
If W= Fg. but the centre of buoyancy (B) is below tentre of gravity (h), the body is in unstable equilibration as shown in fig(b). A slight displacement to the body in the clockwise disceedion to the body. In the clockwise direction, gives the couple due to Way Fig also in the clockwise direction. This the body does not refun to its original position and too hence the body is in unstable equillobrium.

(c) Neutral equilibratum 9—

It FB = W and B and by are at the same point, as shown in big takes, the body is said to be in newhal equilibration.

* Stability of Floating Body =>

The stubility of a bloating body is determined from the position of Meta-centre (M). In case of bloating body, the weight of loguid displaced.



(a) Stable equilibration M is above by

(b) Unistable equilibration of

(Stability of Housing bodies)

(a) Stable Equilibrium:

If the point M is above M is above by, the blooking body will be in stable equilibrium as shown in by (a). It a slight angular displacement is given to the blooking body is the clockwise direction, the Centre of buoyancy shifts from B to B, such that the vertical line through By eats at the then the blooking in the arti-clockwise elinection and thus bringing the blooking in the arti-clockwise elinection and thus bringing the blooking the blooking body in the original position.

(b) Unstable Equilibrium 2

The the point m is below G, the bloating body will be in unstable equilibrium as shown in (b). The disturbing couple is acting in the alcoholise direction. The comple due to buoyant bonce F3 and w is also acting in the clockwise alerection and thus overcturning the bloating body.

is Newtral Equilibrium:

The the point my is out the centre of greavity of the body, the bloating body will be in neutral equilibrium.



TYPES OF FLUID FLOW: -

The bluid flow is classified as a

- (i) Steady and unsteady blows
- (ii) Uniform and non-uniform Hows
- (iii) Laminar and turbulent blows
- (in compressible and incompressible flows
- (N) Rotational and irrectational blows and
- (Ni) One, two or three domensional blows

(1) Steady and Unsteady blows >

Therapy blow is defined as that type of blow in which the blowd Characteristics like volocity, pressure, density etc. at a point do not change with time the bore steady blow, mathematically, we have

whome (xo, yo, zo) is a boxed point in blund bield

The density a respect to time, Thus modhernatically, for unsteady fier

(1) Uniform and Non-Uniform Flows of

Velocity of any given time does not change with respect to space the Congth of direction of the blow). Mosther modically, bore uniform the

where ov = change ob velocity

Bs = Length of blow in the direction s

of Non-Uniterior Blow is that type of blow in which the velocity of ciny given time Changes with respect to space. Thus, mathematically, box non-uniform blow

(Ss) t= constant # D

(iii) Laminan and Turbulent Flow >

- Pareticles move along well-defined paths on steam line and all the steam lines and parallel. Thus the pareticles move in laminas on layers gliding smoothly over the adjacent layer. This type of blow is also called steam-line blow or viseous blow.
- Turbulent blow is that type of blow in which the bluid pandicles move in a zig-zag way. Due to the movement of bluid pandicles on a zig-zag way, the eddies formation tokes place which are responsible for high energy loss. For a pope blow, the type of blow is determined by a non-dimensional number. Called the Reynold number.

where D = Documeter of pipe

N= mean velocity of blow on pipe

V = Kinematic Viscocity of Bluid

laminant. It the Reyland number is more than 4000, then it is called turbulent blow. It the Reyland number is more than 4000, then it is called turbulent blow. It the Reynold number lies between 2000 and 4000, the flow may be laminant on turbulent.

(IV) Compressible and Pricompressible Flows of

"T Compressible blow is that type of blow in which the dentity of the bluid changes brown point to point on in other words the dentity of the bluid. Thus, madhematically, fore (P) is not constant from the bluid. Thus, madhematically, fore (P) is not constant from the bluid. Thus, madhematically, fore (P) is not constant from the bluid.

of & constant

-1) Incompressible blow is thed type of blow in which the density is constant bouthe Bluid blow. Liquids age generally incompressible cohile gases are compressible. Mathematically, box a incompressible blow:

F = constant

(V) Rotational and Pretrotational Flows >

Rotentional blow is that type of blow in which the bluid particles while blowing along steam times, also restates about their can axis. And, it the bluid particles while blowing along steam lines, do not restate about their own axis then that type of blow is earlied innestational blows

Vi) One-, Two-, and Three-Dimensional Flows :-

The dimonstronal blow is that type of blow in which the blow parameter such as velocity is a function of time and one space ephordinate only say at for a steady one, dimensional blow, the velocity is a bunchion of one space. Co-credinate only. The vertication of velocities in other two mutually perpendicular abaction is outstuned negligible. Hence, mathematically, for one-dimensional blow,

u= 5(a), v=0 and w=0

when u, v. and we are velocity components in a, y and z directions mespectively,

Two-observational blow is that type of blow in which the velocity is a faceth bunction of time and two rectangular space co-ordinates or constant say or and y. For a steady two-dimensional blow the velocity is a function of two-space co-ordinate only. The velocity of velocity in the third dimensional blow, negligible. Thus mathematically for two-dimensional blow, it is negligible. Thus mathematically for two-dimensional blow,

-1 Three-dimensional blow is that type of blow in which the velocity is a bunction of time and three mutually perpendicular directions. But bor a steady three-dimensional blow the bluid parameters are bunctions of three space co-ordinates (14, y and 2) only. Thus, mathematically, bor three-dimensional blow, we blow, we be bounded to be blowday.

RATE OF FLOW OR DISCHARGE (Q)

It is defined as the quantity of a fluid blowing per second through a section of a pape on a channel. For an incompressible blood (on location) the node of klow on dischange is expressed as the volume of blood blowing excross the section per second. For compressible bloods of the nate of blow is usually expressed as the weight of blood blowing extrass the section. Thus (i) for loquids the Units of Q are m3/s or latres/s

(ii) for gases the units of Q is kg f /s on Newton/s

Consider a loqued blowing through a pape in which

A = Causs-Sectional area of Pipe

A = Cours - sectional

V= Average velocity of bluid econoss the section

Then Discharge Q = AXV.

CONTINUITY EQUATION ?

The equation based on the principle of Conservation of maks is called Confinulty Equation. That for a blaid blowing through the pipe of all the cross-section, the quantity of blud per second is constant. Consider two enver-sections of a pape as shown in bigues; Let V, = Average velocity at Cross-Section 1-1 -P1 = Density out section 1-1 A = Area of Pipe at Section 1-1

and V21 f21 Az are cornesponding value at section 2.

Then note of blow ed section 1-1= P. A.V.

Right of Stow out Section \$2-2 = P2 Az V2 of Flow According to law of Conservation of TOOSH.

Rede of blow at section 1-1

Fluid blowing through

= Rate of blow out section 2-2

19,A1V1 = P2 A2V2

The above equation is supplicable to the compressible as well as incompressible bluds and is called Continuity Equation. If the blush monoton is incompressable,

then of = f2 and continuity equation revoluces to

A, V1 = A2 V2

EQUATIONS OF MOTION ?

According to Newton's Second low of motion, the net fonce Fix acting on a bluid element in the direction of it is equal to make in of the Bluid element multiplied by the acceleration.

Axin the x-direction,

Thus mathematically; Fx = m-an

In the fluid blow, the following brances are present,

(i) Fg, gravity borce

(ii) fp, the pressure borce

(10) Fr, bonce due to Viscosity.

(i) For borne due to tumbulence

(4) Fc, bonce due to compressibility

Thus in equation, the net boace

Fx = (Fg) n + (Fp) n + (Fv) on + (Fe) at (Fc) x

(i) It the bonce due to compressibility, fe is negligible, the nesulting net boace

Fx = (Fg) nx + (Fp) nx + (Fv) nx + (Fd) n

and equation of motions are called Reynold's equations of motion.

- (ii) For blow, where (F4) is negligible, the mequed equation resulting equations of motion are known as Navier-Stokes Equation.
- (ii) It the blow is assumed to be ideal, this cous borce (Fv) is zero and equation of motions are known as Euler's equation of mation.

EULER'S EQUATION OF MOTION ?

This is equation of motion in which the borce flue to gravity and pressure are taken into consideration. This is dereaved by considering the motion of a bluid element along a stream-line as "

consider a stream-line in which blow is taking place in a discretion as shown on biguine. Consider a Cylindrical element of Cross-section and length dis. The borace acting on the Cylindrical element are

1. pressure bonce pdf in the director of 5000

a. Pressure force (p+ &p ds) dA opposte to the direction of blow, a weight of element padAds.

Let 0 is the angle between the ofinection of blow and the line of action of the weight of element.

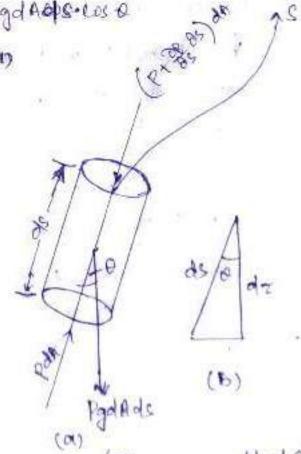
The resultant borcce on the bluid element in the direction of os must be equal to the mass of bluid element X acceleration in the direction s.

= fdAds xas - (1)

where as is the acceleration of S.

Now, $a_s = \frac{dv}{dt}$, where v is a bundom of s and t.

It the flow is steady,



Substituting the value of Cis in agri (1) and simplifying the equation, we get

- OP alsola - Po d'Ads costo - Podads X &

Dividing by PoledA, -- ap -g cos a = vdv

on de + g cos 0 + v dy =0

But from tig(tb), we have cos o = ots

Equation (2) To known as Eulen's equation of motion.

BERNOULLI'S EQUATION FROM EULER'S EQUATION >

Bennoulliss equation is obtained by integrating the Euler's equation of motion as

of blow is incompressible, fire constant and

$$\frac{P}{P} + gz + \frac{v^2}{z} = constant$$

$$\Rightarrow \frac{p}{fg} + \frac{v^2}{2g} + Z = constant \qquad (9)$$

Equation (3) 25 & Berenoulle's equation in which,

Pg = pressure energy per unit weight of third on pressure head

V2/2g = kinetic energy per unit weight on lanetic head Z = potential energy per unit weight on potential head

ASSUMPTIONS :-

The following one the assumptions made in the devilvation of Berenoulli's equation:

(i) The bluid is ridealine. Viscosity is Zeno.

(6) The How is Steady.

(iii) The Blow is in compressible.

(14) The blow is Ircrotational.

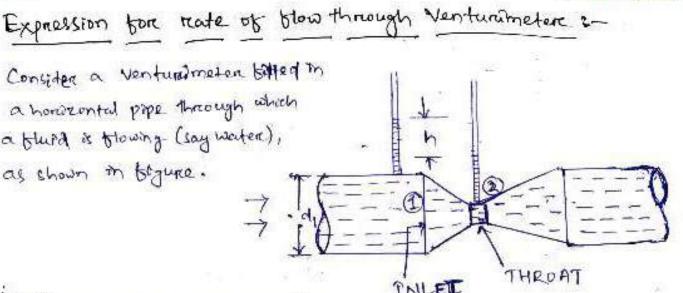
PRACTICAL APPLICATIONS OF BERNOULLI'S EQUATION:

Bernoullis equation is applied in all problems of incompressible blud blow where energy considerations are involved. But we shall consider its application to the bollowing measuring devices:

- 1. Venturimeter
- 2. Orabbice meters
- 3. Pitot tube

(1) Venturimeter =>

- of a bluid blowing through a pipe. It consists of three parts in
 - (1) A short converging point,
 - (1) Throat and (iii) Diverging parit.
- 7 94 his based on the principle of Bernowliss equation.



Let P1 = pressure out section (1)

d1 = eliameter out inlet on out

coction (1).

[VENTURIM ETER]

VI = velocity of bluid on section (1), a = Area at section (1) = 1 4,2

and d2, P2, V2, a2 are courses ponding values at section (2).

Applying Beaumoullist equation at section (1) and (2), we get

As pope is horazontal, hence = Z= Zz

:.
$$\frac{P_1}{P_9} + \frac{V_1^2}{2g} = \frac{P_2}{P_9} + \frac{V_2^2}{2g}$$
 or $\frac{P_1 - P_2}{P_9} = \frac{V_2^2}{2g} - \frac{V_1^2}{2g}$

But PI-Pz is the dibterence of pressure heads at soctions found 2 and it is equal to hore PI-Pz = h

Substituting this value of PIP2 in the above equation, we get

$$h = \frac{V_1^2}{2g} - \frac{V_1^2}{2g}$$
 - (5)

Now applying continuity equation at section 182 a, v = a2 v2 on v, = a2 v2

$$h = \frac{v_2^2}{2g} - \frac{\left(\frac{a_2}{\alpha_1}\right)^2}{\frac{2g}{2g}}$$

$$= \frac{v_2^2}{2g} + \left(1 - \frac{\alpha_2^2}{\alpha_1^2}\right) = \frac{v_2^2}{2g} + \frac{\alpha_1^2 - \alpha_2^2}{\alpha_1^2}$$

$$\Rightarrow v_2^2 = \frac{2gh}{\alpha_1^2 - \alpha_2^2}$$

$$\Rightarrow v_2^2 = \frac{2gh}{\alpha_1^2 - \alpha_2^2} = \frac{\alpha_1}{\alpha_1^2 - \alpha_2^2} + \frac{2gh}{\alpha_1^2 - \alpha_2^2}$$

. Discharge, Q = a2 V2

$$= \frac{a_2}{A_1^2 - a_2^2} \times \sqrt{2gh}$$
=7 $Q = \frac{a_1}{\sqrt{a_1^2 - a_2^2}} \times \sqrt{2gh} - -(6)$

Equation (6) gives the discharge under rideal conditions and is called theoretical discharge. Actual discharge will be less than theoretical discharge.

where ey= co. efficient of Venturismeter and its value is less:
than 1. (co-efficient of discharge)

Value of the givenby different 1) tube manometers >-

Case-1: Let the distremential monometers contains a liquid which is heavier than the liquid blowing through the pipe.

Let Sh = Specific growing of the heavier liquid

So = specific growing of the liquid flowing through pipe

N = Specific growing of the heavier liquid column in U-tube

Case-11: 25 the differential manameters tentains a layured which is lighters. Than the liquid blowing through the pipe, the value of his given by,

h = x [1- se]

Se = specific greatity of bojoinlighter liquid in U-tube

So = specific greatity of blund blowing through Pipe

R = Difference of the lighter liquid columns in U-tube.

Decestions The diameter of pipe at section 1 & 2 and to cm & 15 cm nespectively. Find the directions through the pipe, it the velocity of worker flowing through the pipe of section 1 is 5 m/s. Also determine the velocity at section 2.

Answer: - $d_1 = 10 \text{ cm}, d_2 = 15 \text{ cm} = 3.15 \text{ m}$ $V_1 = 5 \text{ m/s}$ $V_2 = 23$ $Q_1 = 77$

 $\begin{cases}
Q_1 = A_1 \times V_1 \\
= \frac{\pi}{4} d_1^2 \times V_1 \\
= \frac{\pi}{4} (b_1)^2 \times 5 = \frac{\pi}{4} \times b_2^{\frac{10}{10}} \times 5 = 3.141 \times 125 \\
= \frac{\pi}{4} \times (b_1)^2 \times 5 = \frac{\pi}{4} \times b_2^{\frac{10}{10}} \times 5 = 3.141 \times 125$

 $Q_{1} = \frac{11}{4} \times 10.001 \times 5$ $= \frac{11}{4} \times 0.0001 \times 5$ $= \frac{3.141}{4} \times 0.0001 \times 5$ $= 0.0342 \text{ m}^{3}/5$

Then, A, VI = A2V2 0.03.92 0.03.92 0.0392 0.0392 0.0392 0.0392 0.0392 0.0175

The Go cm. diameter pipe in which water is blowing branche, into two pipes of diameter 20 cm. and 15 cm respectively.

Of the average velocity in the 30 cm. diameter pipe is 25 m/s, findout the discharge in the pipe? Also determine 25 m/s, bindout the discharge in the pipe? Also determine the velocity in 15 cm. pipe if the average velocity in 20 cm. the velocity in 15 cm. pipe if the average velocity in 20 cm. diameter pipe is 2 m/s?

Any Given, $d_1 = 80 \text{ cm} = 0.30 \text{ m}$ $d_2 = 20 \text{ cm} = 0.20 \text{ m}$ $d_3 = 15 \text{ cm} = 0.15 \text{ m}$ $V_1 = 2.5 \text{ m/s}$ $V_2 = 2 \text{ m/s}$ $V_3 = 2?$

 $V_2 = 2\pi I_5$ $V_3 = 2?$ $Q_1 = A_1 \times V_1$ $= \frac{\pi}{4} A_1^2 \times V_1$ $= \frac{\pi}{4} \times (0.30)^2 \times 245$ $= \frac{\pi}{4} \times 0.09 \times 2.5 = \frac{3141}{4} \times 0.09 \times 2.5$ $= 0.76 \times 0.09 \times 2.5$

= 0.176 m3/s

In tigune, Q1=Q2+Q3 >> A1V1 - A2V2+A3V3

70-176 = #xd2xv2 + # Txd3 xv3

= \$x 6.20) 2x 2 + \$x (0.15 } x'V3

= 0.78 x 0.04 x 2 x + \$0.78 x 0.0225 x V3

=>0.176 = 0.0624 + 0.0175 xv3

70-196-10.0624 = 0.0175 XV3

1 7 0.1136 =0.0175 XN3

$$V_{3} = \frac{0.1186}{0.0175}$$

$$\Rightarrow V_{3} = 6.4 \text{ m/s} \quad (Ans)$$

$$OR, \quad Q_{1} = Q_{2} + Q_{2}$$

$$\Rightarrow A_{1}V_{1} = A_{2}V_{2} + A_{3}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{1}V_{2} + A_{2}V_{3} + A_{2}V_{3} + A_{3}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{1}V_{2} + A_{2}V_{3} + A_{2}V_{3} + A_{3}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{1}V_{2} + A_{2}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{2}V_{2} + A_{2}V_{3}$$

$$\Rightarrow A_{1}V_{1} = A_{2}V_{1} + A_{2}V_{2}$$

$$\Rightarrow A_{1}V_{1} = A$$

$$V_{AB} = 3m/s$$
 $Q_{AB} = ?$
 $Q_{AB} = ?$
 $Q_{CE} = ?$
 $Q_{CD} = \frac{1}{2}Q_{AB}$
 $Q_{CE} = \frac{1}{3}Q_{AB}$
 $Q_{CE} = \frac{1}{3}Q_{AB}$

Rate of discharge at AB,

$$Q_{AB} = A_{AB} \times V_{AB}$$

$$= \frac{\pi}{4} (d_{AB})^2 \times V_{AB}$$

$$= \frac{\pi}{4} (1.2)^2 \times 3 = \frac{\pi}{4} \times 1.44 \times 3 = 0.76 \times 3 \times 1.44$$

$$= \frac{\pi}{4} (1.2)^2 \times 3 = \frac{\pi}{4} \times 1.44 \times 3 = 0.76 \times 3 \times 1.44$$

$$= \frac{\pi}{4} (1.2)^2 \times 3 = \frac{\pi}{4} \times 1.44 \times 3 = 0.76 \times 3 \times 1.44$$

From bigune, and and QAB = QBC

THANK VAB = ABC X VBC

THE COLARS X X 3 = TX (Close) 2 X VBC

TY (Class) X 3 = TX (Close) 2 X VBC

TY X3 X(1.2) 2 = TX X(1.5) 2 X VBC

=> 3.39 = 1.76 × VBE => VBC = 3.39 = 1.92 m/s 1.76 = 1.76 = 1.92 m/s 1. Velocity in BC is 1-92 m/s Then, Qep = 3 Rm = 3 × 3.39 = 1.131 m3/s

 $Q_{CE} = Q_{AB} - Q_{CD} = 3.39 - 1.131 = 2.262 m^3/5$ OR $Q_{CE} = \frac{2}{3}Q_{AB} = \frac{1}{3} \times 3.39 = 2.262 m^3/5$

Velocity for CD ...

$$V_{CD} = \frac{Q_{CD}}{A_{CD}}$$
 $V_{CD} = \frac{Q_{CD}}{A_{CD}}$
 $V_{CD} = \frac{Q_{CD}}{A_{CD}}$

7 Nep = 2-25 m/s 1. Nelocity in CD is 2.25 m/s

diameter of CE can get from this expression,

we know, Discharge out CE,

QUE = ACEX VCE

7 Que = Tx(die)2 x VCE

> 2.262 = = = x (dec) x 2.5

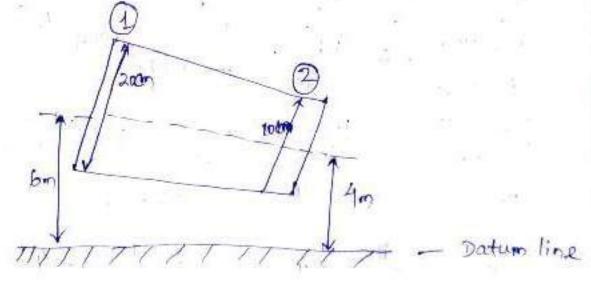
>> 2.262 = (dcs)2 x 1.963

7 (des) = 2.262

= 1-073 m.

: diameter of CE is 1-073 m.

1 Water is blowing through a pipe having diameter 20 cm. & 10 cm at section 122 nespectively. The nate of blow through page is 35 litrefsel. The section 1 is 6 m, above the datum and section 2 is 4 mr above the datum. If the pressure at cross section 1 is 39.24 Alone other bind out the fundencity of pressure out section 2.



Given, d= 20 cm, = 0,20 m Z, = 6m. 0/2= 10 cm, =0,10m = 72=4m. Q= 3545 . . 9 = 9-81 7 Q = 35×10-3 m3/5 f= 1000 kg/m2 P1=39.24 N/cm2 = 39.24 × 104 N/m2. According to Bernoul's equations. +71+ V12 - P2 + Z2+ 129 Q=Q= Q = 35 e/s Q = A, V, 735×10-3= 7×607×4 = Tx(0.20) x Y =0.78 XD.01 XV2 735 X 10 3 = 0.78 KO.04 XV 9 35x 103 = 0.0312 XV 7 0.035 = 0.0312XV Then according to Bennowth equation, >> 2929× 107 + 6 + 1.21 = P2 + 4+ 19.36 9810 + 4+ 19.62 $970+6+0.061 = P_2 + 1+0.986$ $970+6+0.061 = 9810 + 4.986 <math>9 P_2 = 41.075$

$$= 102945.75 \times 9810$$

= 402945.75 N/m²
= 40.29 N/cm² (And)

(B) An oil of specific greavity 0-8 is blowing through a .

Venturimeter having in let cliameter 20 cm. and throught

Venturimeter having in let cliameter 20 cm. and throught

diameter 10 cm. The oil francury differential manameters

diameter 10 cm. The oil francury differential manameters

shows a reading of 25 cm. Calculate the discharge of

shows a reading of 25 cm. Calculate taking cd = 0-98?

(my) Given, of = 20 cm = 0.20 m

$$d_2 = 10 \text{ cm} = 0.10 \text{ m}$$

$$S_{12} = \text{specific growity of oil} = 0.8$$

$$S_{13} = \text{specific growity of mencury} = 13.6$$

$$S_{14} = \text{specific growity of mencury} = 13.6$$

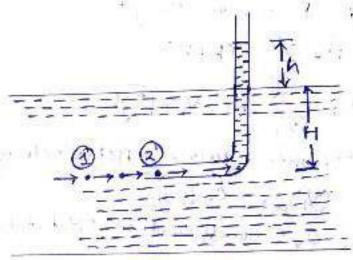
$$S_{15} = \text{specific growity} = 25 \text{ cm} = 0.25 \text{ m}$$

$$S_{15} = \text{specific growity} = 25 \text{ cm} = 0.25 \text{ m}$$

According to case - I,

$$h = \pi \left[\frac{sh}{sn} - 1 \right]$$
= 0.25 x \left(\frac{13.6}{0.8} - 1 \right) = 0.25 x (17-1) = 0.25 x 16
= 40 cm

It is a device used for measuring the velocity of blow at any point in a pipe or a channel . It is based on the principle point in a pipe or a channel . It is based on the principle that it the velocity of blow at a point becomes zero, that it the velocity of blow at a point becomes zero, that it the pressure there is increased due to the conversion of the kinetic energy into pressure energy. In its simplest form, the pitot-tube consists of a glass tube, bent at rught angles as shown in biguire.



Pitot-tube

The lower and, which is bent through 90° is directed in the up steam direction as shown in figure. The liquid rises up in the tube due to the conversion of kinetic energy into pressure energy. The velocity is determined by measuring the rise of liquid in the tube.

Consider two points (1) and (2) at the same level in such a way that point (2) is just as the inlet of the pitot-tube and point (1) is bak away from the tube.

Let P1 = intensity of processure cut point (1)

M = velocity of flow at (1)

P2: processure at point (2)

V2 = velocity out point (2), which is Zero

H = elepth of tube in the liquid

h = rise of liquid in the tube cubove the free surface.

Applying Bernouti's equation at points (1) and (2), we get

$$\frac{P_1}{P_0} + \frac{\sqrt{2}}{29} + Z_1 = \frac{P_2}{P_0} + \frac{\sqrt{2}}{29} + Z_2$$

But $Z_1 = Z_2$ as points (2) and (2) are on the same line and $V_2 = 0$
 $\frac{P_1}{P_0} = \text{pressure head at (1)} = H$
 $\frac{P_2}{P_0} = \text{pressure head at (2)} = (h+H)$.

Substituting these values, we get

 $H + \frac{\sqrt{2}}{29} = (h+H)$
 $h = \frac{\sqrt{2}}{29}$ ore $V_1 = \sqrt{29}h$

This is the prefical invetocity. Actual velocity is given by

 (N) and $= C_1 \sqrt{29}h$

where $C_1 = C_2 \sqrt{29}h$

:. velocity at any point

v= Crvzgh

3 CHAPTER -05 ORIFICE

Introduction ?

Orelifice is a small opening of any cross-section (such as cineular the angular exceedingular etc.) on the side on at the bottom of a tank, through which a bluid is blowing. A mouth piece is a short length of a pape which is two one to three times its diameter in length, kitted in a tank on vessel containing the bluid. Draffices as well as mouth preces are used for measuring the rade of flow , of bluid.

Classification of Driftices >

The onlitices one classified on the basis of their size, shape, nature of discharge and shape of the upsteam edge. The tollowing are the important classifications:-

- (1) The onlyices one classified as small orders on large onlyice depending upon the size of onlifice and head of liquid from the Centre of the orapice. It the head of liquid from the centre of trifice is more than tive times the depth of priffice, the orifice is called small onlyfice. And it the head of liquids is less than five times the depth of prefice, it is known as large online.
- 2) The orifices one classified as (i) Cincular orifice,
 - (ii) Tritangulare onifice (iii) Rectangulare onifice and
 - tivi Square profice depending upon their Cross-sectional arreas
- 3) The onlifees one classified as (1) shortprediged onlifee and a (ii) Bell-mouthed onifice depending upon the shape of cupstream edge of the onligitus.

(4) the orabices are classified as

(i) Free discharging orifices and (ii) Drawned on sub-mercyed correspond to nothing upon the nothing of discharge.

The submerged orifices one burther chustised as (a) fully submerged orifices and (b) partially submerged orifices.

Flow through an Onifice of Consider a tank bitted with a circular onlyice in one ist its eides as shown in bigune.

Let the the head of the liquid subove the centre of the omitice. The liquid whose the liquid blooding through the original borons a jet of liquid whose area of cross-section is less than that of original the area of jet of bluid gloss on decreasing and at a section &-C, the area is minimum. This section is approximately at a distance of half of minimum. This section is approximately at a distance of half of diameter of the original to each other and perpendicular to the straight and portalled to each other and perpendicular to the plane of the original. This section is called Vena-Contracta. Beyond this section, the jet diverges and is attracted in the downward direction by the gravity.

Consider two points I and 2 as showing in bigure. Point I is inside the tank and point 2 at the Vena-Contracta, Let the blow is steady and at a Constant head H. Applying Bernoutile equation at point.

Jet of blund

(Tank with an onitice)

But
$$\frac{P_1}{\sqrt{g}} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\sqrt{g}} + \frac{V_2^2}{2g} + Z_2$$

$$\frac{P_1}{fg} + \frac{V_1^2}{2g} = \frac{P_2}{fg} + \frac{V_2^2}{2g}$$

Vi is very small in comparison to ve as area of tank is very large as compared to the area of the Set of liquid.

This is theoretical velocity. Actual Velocity will be less than this value.

HYDRAULIC CO-EFFICIENTS >

The hydraulic co-applicants are 1-

1] Co-abbicient of velocity, ev

2] co-efficient of Contraction, Ce

3) Co-efficient of discharge, Co

(4) Co-efficient of Velocity (Cv):-

It is defined as the nation between the actual velocity of a set of liquid at vena-Contracta and the theoretical of set.

Out is denoted by Evi and mouthematically inch is given as

Cv = Actual relocity of set at venar contracta.

Theoretical velocity

= vagit , where V= actual velocity, vaget = Theoretical velocity

The value of Co varies brown 0.95 to orga for different orifices, depending on the shape, size of the Orifice and on the head under which blow takes place. Generally, the value of Co=0.98 is taken for sharp-redged orifices.

(2) Co-efficient of Contraction (Cc):-

It is defined as the reaction of the carea of the jet at vena - Contracta to the area of the brifice. It is denoted by Co.

Let a = area of briffice rand

ac = area of Jet at Vena-Contracta

area of Jet at vena-Contracta

area of Driffice

area of Driffice

The value of Co varies from 0.61 to 0.69 depending for shape and size of the oratice and head of liquid under which flow takes place . In general the value of Co may be taken as 0.64.

(3) Co-efficient of Discharge (Cd):-

It is defined as the receipt of the actual discharge trum an orcifice to the theoretical discharge from the orcifice. It is denoted by Cd. It @ actual discharge and Qth is the theoretical discharge then mathematically, Cd is given by Cd = Q - Actual velocity x Actual Area

Cd = Q - Actual velocity x Theoretical area

- Actual velocity x Actual Area

Theoretical velocity x Actual Area

Theoretical velocity Theoretical area

the value of Col variety from 0.61 to 0.65. For general purpose the value of Col is decken as 0.62.

NOTCH

Introduction :-

A notch is a device used for measuring the reade of flow of a higher through a small channel on a tank. It may be defined as an opening in the side of a tank or a small channel in such a really that the liquid surface in the tank or channel is below the top edge of the opening.

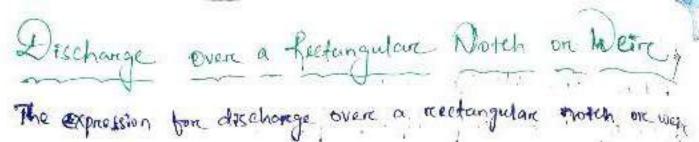
A wein is a Concrete on maionary structure, placed in an open channel over which the flow occurs. It is generally in the form of verdical wall, with a sharp edge cut the top, running all the way across the open channel. The notch is of small size while the wein is of a bigger size. The notch is of small size while the wein is of a bigger size. The notch is generally made of metallic plate while wein is made of Concrete or masonary structure.

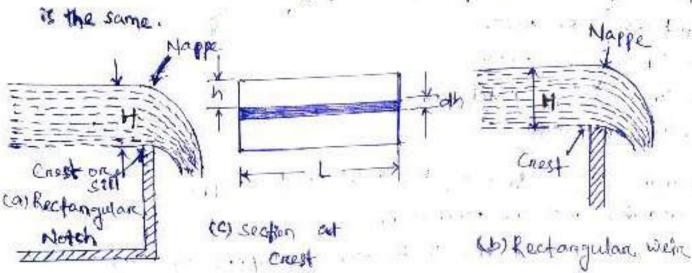
1. Nexpec on Vein: - The sheet of water flowing through a notch

2. Chest on the bottom edge of a notch on a top of a weign over whach the wester flows, is known as the Classification of Notes and weires ?

The notches aree classified as :

- (1) According to the shape of the opening:
 - (a) Rectangular notch
 - (b) Trixingulare notch
 - (c) Trapozordal noteh and-
 - (d) stepped notch
- (2) According to the effect of the sides on the nappe:
 - cas Notch with end contraction
 - (b) Notch without end contraction on suppressed notch
 Weine are classified according to the shape of the opening, the
 shape of the Creek, the about of the side on the nappe and
 nature of discharge. The following are important classification.
 - (a) According to the shripe of the opening:
 - (i) Rectangular wein
 - (18) Tritangulare were and
 - (in) Thapezordal wein (Cipalletti wein)
 - (b) According to the shape of the crest:
 - (1) Sharp-enosted wellow
 - (15) Broad-Crested weir
 - (ti) Nannow-Crested wein and
 - (14) Dejae Shaped wetre
 - (c) According to the effect one sides on the emerging nappe;
 - (i) Well with end contraction and (i) Well without end





(Rectangulare notch and weire)

Consider a rectangular notch on we're provided in a channel carrifing water as shown in figure.

Lef H= Head of water over the const L= Length of the notch on work

For finding the dischange of water flowing over the weir on noth, consider an elementary horizontal estrop of water of thickness of and length L at depth h from the free & surface of water is shown in bigure.

The area of strip = Lxdh

and theoretical velocity of water blowing through strip = Tagh

The discharge de, through strip is

de = Cd x Area of strip x Theoretical Velocity

= Cyx Lx dh x vzgh

where Col = co-effectent of closchange

rihe total discharage. Or, for the whole noteh on wein is defermined by integrating equation (i) between the limits 'D and H . :. Q = 5th Carl. 129h dh = CAXLX VZg St hV2dh = Cax Lx/2g [h/2+1] = CdxLx \sq \[\frac{h^{3/2}}{3/2} \] H = 3 Cox LX (29[H]3/2 Vischange Over a Triangular Notch on Weire of The expression for the discharge over a triangular notth on wein is the same. It is the derived as: Let H = head of water above the V-notch O= angle of notch . Consider a horizontal strip of water of threeness did at a depth of h from the bree surface of water as shown in figure. Box September . from figure (b), we have tan = AC = AC· AC = (H-h) tan 0 width to strip = AB = 2AC = 2 (H-h) tan 0/2 As

: Accord strip = 2(4-h) fan 0/2 x dh

The theoretical velocity of water through strop= \agh

Discharge, through the strop,

de = Cox Area of strop x velocity (theoretical)

= Cd x a(H-h) tan 0/2 x dh x vagh

= 2Cd & (H-h) tan 0/2 x gh x dh

Total discharge,

Q = \int 2Cd (H-h) tan 0/2 x vagh x dh

= 2Cd x tan 0/2 x vagh x dh

= 2Cd x tan 0/2 x vagh x dh

= 2x cd x tan 0/2 x vag \int (H-h) h va dh

= 2x cd x tan 0/2 x vag \int (Hh) va - h va dh

= 2x cd x tan 0/2 x vag \int \int (Hh) va - h va dh

= 2x cd x tan 0/2 x vag \int \int \int (Hh) va - h va dh

= 2x Cd x tan 8/2 x 2g [Hh3/2 - h 6/2] H = 2x Cd x tan 8/2 x 2g [3/4 + H3/2 - 2/5 H5/2] = 2x Cd x tan 8/2 x 2g [3/4 + H3/2 - 2/5 H5/2] = 2x Cd x tan 8/2 x 2g [4/5/2] 3/5/2] = 8/6 Cd x tan 8/2 x 2g [4/15 H5/2] = 8/6 Cd x tan 8/2 x 2g x H5/2

For a right angled V-notch if $C_d = 0.6$ $0 = 90^\circ$, i.tan 0/2 = 1

Discharge, Q = 8 x 0.6 x 1 x \2x9.81 x H5/2 = 1.417 H5/2

Loss of Energy in pipes ?

When a bluid the blowing through a pipe, the bluid expendences some resistance due to which some of the energy of bluid is lest. This loss of energy is classified as:

Energy losses

1

This is due to brickion and it is calculated by the bollowing formulae 1

formulae:
(a) Dancy- weis bach formula (c) Bond in pipe

LMajor Energy losses . . . 2 Minon Energy bosses

This is due to (a) Sudden expansion

(b) Sudden Contraction

. .

LOSS OF Energy (OR HEAD) DUE TO FRICTION &

19) Dancy - Wessbach Foremula :-

The loss of head (on energy) in purpose pipes due to furction is calculated brom Dancy-weisbach equation which has been derived in chaptere to and is given by $h = 4.5 \cdot L \cdot V^2$

 $h_{\xi} = \frac{4. \, \xi \cdot L \cdot V^2}{91 \times 29}$

where he = 1035 ob head due to briction,

by = co. afficient of bruction which is a function of, Reynold's number.

= 16 for Re W 2000 (VOSCOUS Blow).

= 114 for Re Varying from 4000 to 106 L = length of pipe V = mean velocity of blow d = doameter of pape (b) Chezy's Foremula fore loss of head due to bruietion in pipes: Retent to Chapter to auticle to in which expression born loss of head due to britation in people pipes is derived. . Equation (187) of audicle to ho F to x P x LX V2 where he = loss of head due to batchion -P = welted personeten of fire A = Area of crease-section of pipe 1. Lastength of Pope V= mean velocity of blow Now the realto of P (Area of blow) is called hydrauly mean depth on hydroulic reading and is denoted by m. tydraudic mean depth, m = A = 30 = d Substituting . A = m on P = in equation (2), we get. ht = by x Lx v2x from v2 = htx fg xmx & L The state of the open = fg xmxhb JA L (FLXWX WE. = 1 13 (3). Let 19 = c, where c is a constant known as chezy's constant and the = i, where is is loss of shead per unit length of pipe substituting the values of 199 and to in equation = (3)
we get . V = CVmi . (4).

regulation. (4) is known as Cherry's borimula. Thus the loss of head due to briction on a in pipe broom cherry's borimula can be obtained it the velocity of blow through pipe and also the value of C is known. The value of m for pipe is always equal to other of 4.

MINIOR ENERGY (HEAD) LOSSES 7

The toss of head on energy due to friction in a prope is known as major loss while the loss of energy, due to change of velocity of the bollowing bluid in magnitude on direction is called minor boss of energy. The minor loss of energy (on head) includes the bollowing cases:

- 1. Loss of head due to sudden enlargement,
- 2. Loss of head due to Sudden conficaction,
- 3. Loss of head stacks at the entrance of a pipe.
- 4. Loss of head out the exit of a pipe
- 5. Loss of head due to an obstruction in a gipe,
- 6. Loss of head due to bend in the pape.
- 7. Loss of head in Marrious pipe bittings.

In case of long pape the above losses are small as compared with the loss of head due to briction and hence they are called minor losses and even may be neglected without serious error. But in case of a short pape, these losses are comparable with the loss of head due to friction.

HYDRAULIC GRADIENT AND TOTAL ENERGY LINE ?

The concept of hydroculic greatient line and total energy line is very useful in the study of the blow of blueds through pipe. They are defined as:

Hydraulic Gradient Line ?

It is defined as the line which gives the sum of pressure. Adad (P) and datum head (Z) of a flowing bluid in a pope with respect to some reference line on it is the line which is obtained by Joining the top of all ventical ordinates, showing the pressure headleplus) of a flowing bluid in a pipe from the centre of the pipe. It is briefly written, as they. Chydraulic (gradient line).

Total Energy Line 7

It is defined as the time which gives the sum of pressure head obtained and kinetic head of a blowing blund in a pipe with respect to some reference line. It is also defined as as the line which is obtained by soining the tops of all verdical ordinates showing the sum of pressure head and kinetic head from the Centre of the pipe.

It is briefly written as T.E.L. (Total Energy Line).

Introduction 7

The loquid comes out in the bound of a Jet broom the outlet 'Of a nozzle, which is the bitted to a pipe through which , the thirt liquid is blowing under pressure. It some plate, which may be fixed on moving, is placed in the path of the Jet, a force is exercted by the Jet on the plate. This bonce is obtained from Newton's 2nd law of motion or from impulse-momentum equation. Thus impact of Jet means the force exerted by the jet on a plate which may be stationary or moving. In this Chapter, the following cases of the impact of jet ine. the force exercted by the jet on a plate, will be considered.

3

- (1) Force exerted by the set on a stationary plate when (a) place is viertical to jet
 - (b) plate is inclined to the jet, and
 - (c) plate is curved.
- (a) Place exercted by the set on a moving place, when

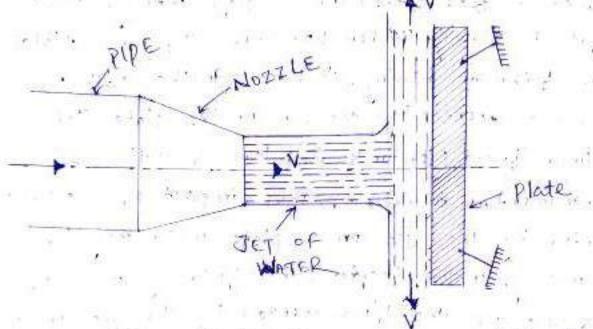
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the form the first product of the second

- (a) place is ventical to viet,
- (b) plate is inclined to the Jet and
 - (c) plate is curved.

Force Exerded By The Jet On a stationary Ventical Plate 7

Gonsider a Jet of water coming out from the nozzle, strukes a blat vertical plate as shown in the below figure.



(Force exerded by set on ventical plate)

Let V = velocity of the jet

de diameter of the jet

a = anea of chois section of the Jet = # 92

The Jet abten straining the plate, will move along the plate:

But the plate is at right angles to the jet.

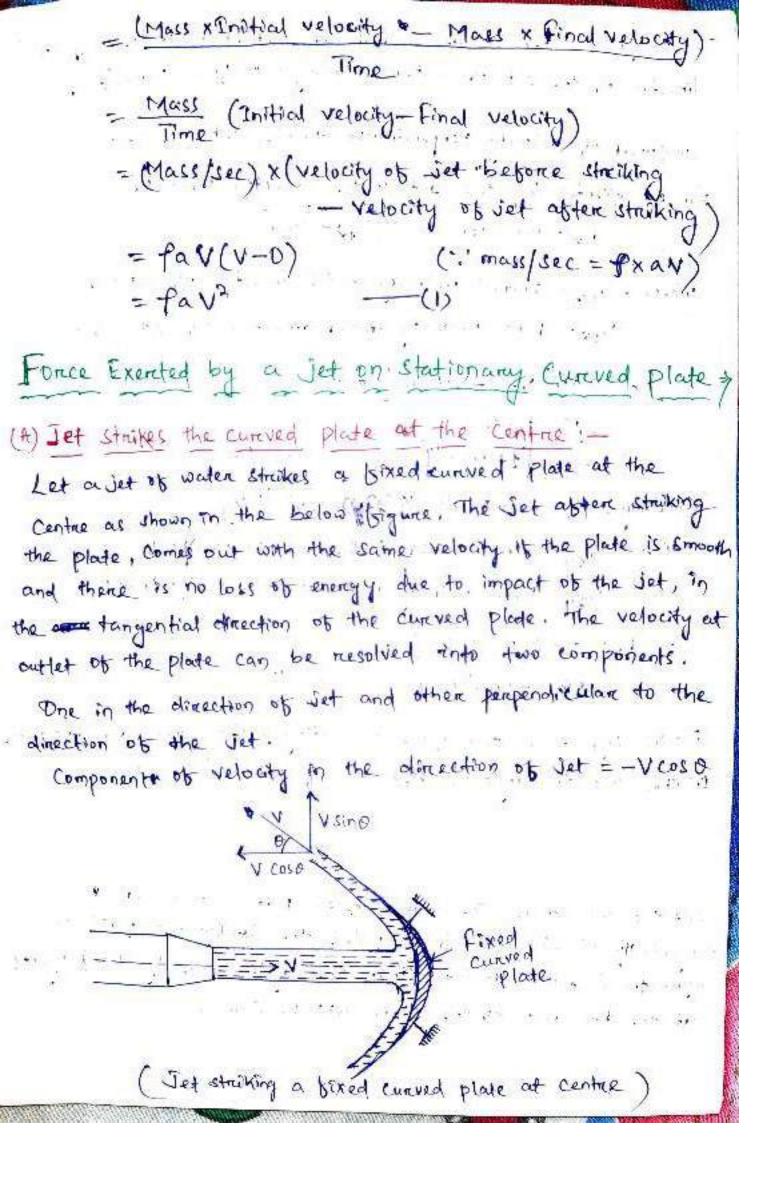
Hence the jet abten A Straining, will get deflected through 90° Hence the Component of the velocity of jet in the direction of Jet, after straining will be zero.

The bonce exented by the set on the plate in the direction of set.

Fx = Rate of change of momentum in the direction of force

Initial momentum - Final momentum

Time



(-ve sign is taken as the velocity at outlet is in the opposite direction of the let of water coming out from Nozzle).

Component of velocity perpendicular to the let = V sin o-

Forced exerted by the viet in the direction of viet,

Fx = mass per sec x[V1x - V2x]

where, $V_{2X} =$ Initial velocity in the direction of Jet = V $V_{2X} =$ Final velocity in the direction of Jet = -V cos a

= fav[v-(-v(0))] = -= fav[v+v(0)] = -= fav2[1+(0)] - (3)

Similarly, Fy = mass part sec x 2 V2y - V2y]

where $V_{xy} = \text{Enitial Valority in the direction of } y = D$ $V_{xy} = \text{Final Valority in the direction of } y = V \text{ sin } D$

 $F_{y} = f_{a}v_{0} - v_{smo}$ $F_{y} = f_{a}v_{smo} - G_{s}$

2 - Ve sign means that borce is acting in the downward director. In this case the angle of deflection of vet = (1500-0)

(B) Jet Strikes the Curved plate cut one end tangentially when the plate is symmetrical;

Let the Jet Striker the Curved bixed plate at one end & tangentially as shown in tigore. Let the concurred plate is symmetrical about straxis. Then the angle made by the trangent at the two ends of the plate will be some.

Let V= valocity of Jet of water

D= Angle made by jet with x-axis

at inlet tip of the curved plate

If the Plate is Smooth and loss

of energy due to impact is Zerro,

then the valocity of water & at the

outlet tip of the curved plate will be

equal to V. The forces exerted by the

Jet of water in the dimensions of

a and y are

\[\text{Fx} = \text{(mass | Sec)} \text{x} \text{[Vix} - Vax] \]

= \text{fa V [V cos a - (-V cos a)]}

= \text{fa V [V cos a + V cos a)}

= 2\text{fa V^2 cos a} \quad - (4)

Fy = fav [Viy-Vay]

= fav [vsina - vsina] = 0

Jet struking curved bixed plate at one and

TNSINO

(C) Jet strikes the Curved plate at one end tangentially when the plate is unsymmetrical:

When the curved plate is unsymmetrical about X-axis, then angle made by the tangents dreawn at the inlet and outlet tips of the plate with x-axis, will be alitherent.

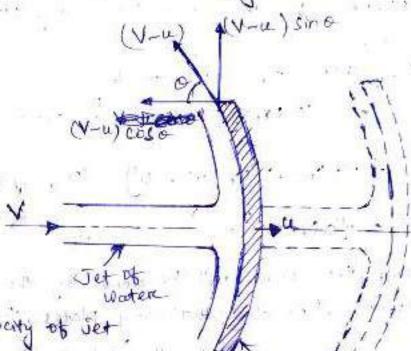
Let 0 = angle made by tangent at inlet tip with X-axis.

The two components of the velocity cut inlet core

Vix = V cos 0 and Viy = V sin 0.

Force on the Cureved Plate when the plate is moving in

Let a jet of water strukes a Curved plate at, the Centre of the plate which is moving with a uniform velocity in the direction of the viet as shown in the figure.



Ket V = Absolute velocity of Jet

a = onea of Jet

u = velocity of the plate ! !

in the direction of the viet

curryed.

Jet straking a Curved moving

The velocity with which jet strikes the curved plate = (V-u).

- It place is smooth and the loss of energy due to impact to jet is Zeno, then the velocity with which the jet will be too leaving the Curved Vane = (V-u).
- This velocity can be restored into two components, one in the direction of the Jet and other perpendicular to the direction of the Jet

component of the velocity in the direction of ordet = - (V-u) cosa

(ve sign is taken as at the outlet, the component is in the opposite direction of the vet).

component of the velocity in the direction perspendicular to the direction of the Jet = (V-u) sin a

Mass of the water struking the plate

= fx a x velocity with which jet strukes the plate

= fxa(V-u).

. Fonce exemped by the jet of water on the cureved plate in the direction of the jet,

Fx = mass stricking pensec X [Enitial velocity with which wet strickes the place in the direction of wet - Final velocity]

= fa (v-u) [(v-u) - (-(v-u) cos o)] = fa (v-u) [(v-u) + (v-u) cos o]

= fa (v-u)2 [1+cos 0] . - (9)

Workdone by the set on the plate per second

= Fx x Distance travelled per second in the direction

The state of the s

 $=F_X \times u$

= fa(v-u)2[1+ cos o] u

= fa (v-w)2 x u [1+cose] - (10)

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the complementary was a series of the complementary was a series of

Force Exercted by a Jet of Water on an Unsymmetrically Moving curved plate on when Jet strukes Tangentially

The above figure shows a jet of water struking a moving curved plate (also called vane) tangentially, at one of its tips. As the jet strukes tangentially, the loss of energy due to impact of the jet will be zero. In this case as plate is moving the velocity with which jet of water strukes is equal to the relative velocity of the jet with respect to the plate. Also as the plate is moving in different direction of the jet, the relative velocity of will be equal to the western object or difference of the velocity of will be equal to the western object or difference of the velocity of the plate at inlet.

Let $V_1 = Velocity of the viet at inlet

[u] = Velocity of the plate (Vane) at inlet

Vr.s = Relative velocity of viet and plate at inlet$

of motion of the plate, also called guide blade angle

D = Angle made by the relative velocity ("Virg) with the direction of motion at inlet also called Nane angle at inlet

Vive and Vig = The components of the velocity of the jet V1, in the direction of motion and perspendicular to the direction of motion of the Vane respectively.

Vw1 = It is also known as velocity of whitel at inlet

Vo1 = It is also known as velocity of blow at inlet

V2 = velocity of the list, leaving the vane on velocity of list

at outlet of the vane.

lez = Nelocity of the Vane at outlet

Vrz = Relative velocity of Jet with respect to the vane at outlet

B = Angle made by the vetocity V2 with the direction of the vane at outlest.

\$\phi = Angle made by the relative velocity (Vaz) with the direction of motion of the Vane of Dutlet and also be called vane angle at Dutlet

Vwa and Vta = Components of the velocity Vz, in the direction of motion of vane and perpendicular to the direction of motion of vane at outlet

Vwa = It is also called the velocity of whire at outlet

'Vrz = Velocity of 61000 at outlet